




# Leveraging IPDAE's New Matrix Instructional Suite to Improve Outcomes

INSTITUTE FOR THE PROFESSIONAL DEVELOPMENT OF ADULT EDUCATORS



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# Welcome

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Workshop Facilitator



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Agenda

- 1:**  
Changes in the Curriculum Frameworks
- 2:**  
The New Adult Education Curriculum Framework for ABE Mathematics
- 3:**  
The New Mathematics Standards Matrix
- 4:**  
The Electronic Mathematics Matrix and Activity Resources

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Our Vision

**YOUR WAY**  
*Florida Adult Education*

**To be the Top 10 Global Economies by 2030**

The slide features a map of Florida and parts of Georgia and Alabama. A pushpin is placed on the map over the state of Florida. The text 'YOUR WAY' is prominently displayed in large, bold, black letters with a colorful arrow pointing right. Below it, 'Florida Adult Education' is written in orange. At the bottom, the vision statement 'To be the Top 10 Global Economies by 2030' is written in bold black text.

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Our Mission

HOW DO WE **GET THERE?**

The slide features the IPDAE logo and the text 'Our Mission' in the top right corner. The central text asks 'HOW DO WE GET THERE?' with 'GET THERE' in large, bold, black letters and a colorful arrow pointing right. Below the text is a collage of four images: a man in a lab coat working on a medical mannequin, a man and woman working at a computer, a woman smiling, and a woman sitting at a desk.

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Rationale


**Background**

Florida [Executive Order 19-32](#) outlines a path for the state to improve its education system by eliminating Common Core and paving the way for Florida students to receive a world-class education to prepare them for jobs of the future.

As a result, the [Florida K-12 B.E.S.T Standards](#) were [written and adopted](#).


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**Curriculum Frameworks Changes Overview**

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Rationale

### New Adult Education Standards


Several design considerations were applied to update the standards.

**Organization & Terminology:** The new ABE standards use the organization and terminology of the K-12 B.E.S.T. standards, which means that overall, there are fewer strands.

**Combining Standards:** Because each ABE level is equivalent to more than one K-12 grade level, some redundant or overlapping standards in B.E.S.T. were combined. In these instances, the B.E.S.T. benchmark that more comprehensively encompassed the breadth and depth of skills was adopted.

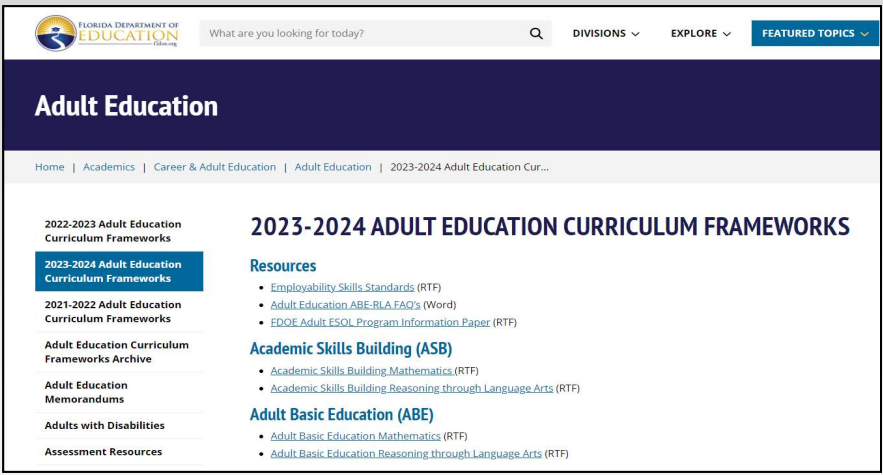
**Levels:** When content appears in K-12 B.E.S.T. but at a different level, the content was kept at the same level as in the previous ABE framework to support consistency with current instruction and assessments.

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Accessing Curriculum Frameworks

### New Adult Education Curriculum Frameworks



The screenshot shows the Florida Department of Education website. The main heading is '2023-2024 ADULT EDUCATION CURRICULUM FRAMEWORKS'. Under 'Resources', there are three categories: 'Employability Skills Standards (RTF)', 'Adult Education ABE-BLA FAQ's (Word)', and 'FDOE Adult ESOL Program Information Paper (RTF)'. Below that are 'Academic Skills Building (ASB)' with 'Academic Skills Building Mathematics (RTF)' and 'Academic Skills Building Reasoning through Language Arts (RTF)'. Finally, 'Adult Basic Education (ABE)' with 'Adult Basic Education Mathematics (RTF)' and 'Adult Basic Education Reasoning through Language Arts (RTF)'. A navigation menu at the top includes 'Home', 'Academics', 'Career & Adult Education', 'Adult Education', and '2023-2024 Adult Education Cur...'. A search bar and dropdown menus for 'DIVISIONS', 'EXPLORE', and 'FEATURED TOPICS' are also visible.

<https://www.fldoe.org/academics/career-adult-edu/adult-edu/2023-2024-adult-edu-curriculum-framewo.stml>

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Reasoning through Language Arts

**Reasoning through Language Arts (RLA) combines both the ABE Reading and ABE Language frameworks into one.**

Previous ABE Frameworks	2023-2024 ABE Framework
Reading	Reasoning through Language Arts (RLA)
Language Arts	
Applied Academics for Adult Education (AAAE)	Academic Skills Building - RLA

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Reasoning through Language Arts

**What's new in RLA?**

- More continuity and clear vertical progressions
- Simpler, more concise language
- Speaking and listening skills are integrated
- Several new benchmarks, including rhetoric and handwriting

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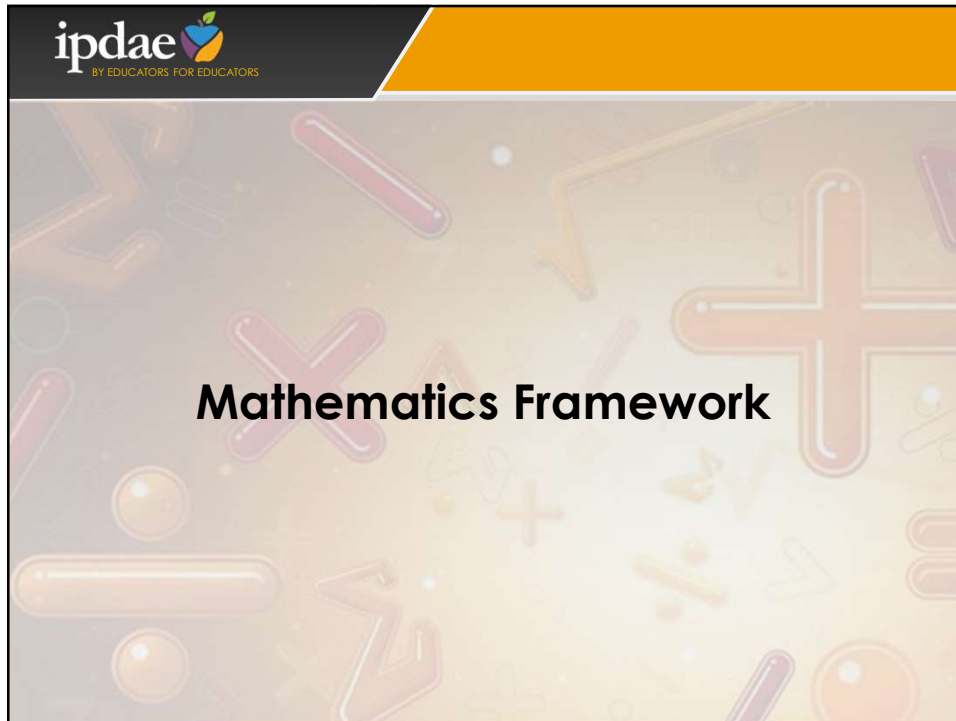


Reasoning through Language Arts

**What's been consolidated?**

Previous ABE Strands	2023-2024 ABE Strands
Foundations	Foundations
Reading	Reading
Writing	Communication
Language	
Speaking & Listening	
	Vocabulary

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The slide has the IPDAE logo in the top left and the word "Mathematics" in the top right. Below the header is a table comparing previous frameworks with the new one. The table has two columns: "Previous ABE Frameworks" and "2023-2024 ABE Framework".

Previous ABE Frameworks	2023-2024 ABE Framework
ABE Mathematics	ABE Mathematics
Applied Academics for Adult Education (AAAE)	Academic Skills Building – Mathematics

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Mathematics

What's new in Math?


- Addition of the Mathematical Thinking and Reasoning Standards to describe the mathematical habits of mind that students should develop alongside their understanding of the content.
- Fluency expectations start earlier and are emphasized throughout
- Overall, there are fewer strands.

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Mathematics

Previous ABE Strands	2023-2024 ABE Strands
Number and Operations: Base Ten The Number System	Number Sense and Operations (NSO)
Number and Operations: Fractions	Fractions (FR)
Operations and Algebraic Thinking Expressions and Equations Ratios and Proportional Relationships	Algebraic Reasoning (AR)
Function	Function (F)
Measurement and Data	Measurement (M)
Geometry	Geometric Reasoning (GR)
Statistics and Probability	Data and Probability (DP)

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Mathematics

Underlying Principles

The framework emphasizes the importance to students:

- Applying math to solve real world problems
- Making connections between and across grade level standards
- Building their conceptual understanding as well as their procedural fluency

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Mathematics

ABE Mathematics Strands, NRS Levels, and Grade Equivalents				
Strands	Basic		Intermediate	
	NRS Level 1	NRS Level 2	NRS Level 3	NRS Level 4
	GE 0 – 1.9	GE 2.0 – 3.9	GE 4.0 – 5.9	GE 6.0 – 8.9
Number Sense and Operations				
Fractions				
Algebraic Reasoning				
Measurement				
Geometric Reasoning				
Data and Probability				
Function*				

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Previous ESOL Framework	2023-2024 ESOL Framework	
Adult English for Speakers of Other Languages (ESOL)	Adult English for Speakers of Other Languages (ESOL)	
Adult ESOL Literacy Skills		
English Literacy for Career and Technical Education (ELCATE)	Academic Skills Building - RLA	
Adult ESOL College and Career Readiness		

*ELCATE is Integrated Education and Training (IET).*

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**Adult ESOL**

**What’s new in ESOL?**

- Literacy Skills are integrated for seamless transition
- Provides civic standards to support Integrated English Literacy and Civics Education (IELCE)
- Integration of English Language Proficiency Standards (ELPS) and ABE Reasoning through Language Arts (RLA)


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**Adult ESOL**

Previous ESOL Frameworks	2023-2024 ESOL Blueprints
ABE Reasoning through Language Arts (RLA) Standards	ELP Standards and ABE RLA Standards (Combined)
English Language Proficiency (ELP) Standards	
FDOE Life and Work Competencies	FDOE Life and Work Competencies
	ESOL Literacy Skills
	Civics Standards

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Adult ESOL

**Underlying principles**


The framework emphasized the importance of students:

- Having the necessary prerequisites literacy skills
- Gaining basic life and work knowledge and skills
- Providing the rights and responsibilities of civic participation
- Acquiring the reading, writing, listening and speaking skills necessary to achieve postsecondary and career goals
- Emphasizing academic language needs

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Challenges Facing Adult Educators




**What are the challenges preventing us from realizing our vision?**

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Challenges Facing Adult Educators



- Time
- instructional Resources
- Guidance and Support
- Assessments
- Varying Achievement Levels
- Absenteeism
- Open Enrollment
- Limited Achievement
- Changes

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The New  
Instructional Matrix Suite

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The image displays three main matrices from the IPDAE suite:

- Florida Adult Basic Education Mathematics Standards Matrix:** Lists standards for Number Sense and Operations (NSO), Fractions (FR), Algebraic Reasoning (AR), and Comperative Reading (CR).
- Florida Adult Basic Education Reading Language Arts Standards Matrix:** Lists standards for Reading Informational Text, Central Idea, Purpose and Perspective, Argument, Connecting Ideas, Reading Across Genres, Interpreting Figurative Language, Paraphrasing and Summarizing, and Understanding Rhetoric.
- Florida Adult English for Speakers of Other Languages Standards Matrix:** Lists standards for English Language Proficiency (ELP) and English for Speakers of Other Languages (ESOL).


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## What Does It Do?

### A One Page Version

- Summarizes several pages of the frameworks
- Includes all NRS Levels
- Includes all strands
- Includes all content standards (abridged)
- Includes all benchmarks (abridged)

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New Standards Matrices

## Electronic Curriculum Matrix

An online lookup tool that dynamically returns resources that are correlated to Florida's adult education framework standards.

### 3 Matrix Types

Look Up Related Activity Resources by:

#### RLA

- NRS Level
- Strand
- Standard
- Benchmark


#### MATH

- NRS Level
- Strand
- Standard
- Benchmark

#### ESOL

- ESL Level
- ELP Anchor Standards

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Vertical Progression


		NRS Level 1	NRS Level 2	NRS Level 3	NRS Level 4
Number Sense and Operations (NSO)	NSO.1	MAL1.NSO.1 Understand the place value of two-digit whole numbers.	MAL2.NSO.1 Understand the place value of four-digit whole numbers.	MAL3.NSO.1a Understand the place value of multi-digit numbers. MAL3.NSO.1b Understand the place value of multi-digit numbers with decimals to the thousandths place.	MAL4.NSO.1a Understand negative numbers and absolute value. MAL4.NSO.1b Rewrite rational numbers in equivalent forms (including fractions, mixed numbers, repeating decimals, and percentages) to solve mathematical and real world problems.
	NSO.2	MAL1.NSO.2 Understand addition and subtraction with one- and two-digit whole numbers.	MAL2.NSO.2 Add and subtract multi-digit whole numbers. Understand multiplication and division operations.	MAL3.NSO.2a Understand operations with multi-digit numbers including decimals. MAL3.NSO.2b Add, subtract, multiply and divide multi-digit numbers.	MAL4.NSO.2 Add, subtract, multiply and divide rational numbers. MAL4.NSO.3 Apply properties of operations to rewrite numbers in equivalent forms.
	NSO.3				
Fractions (FR)	FR.1		MAL2.FR.1 Understand fractions as numbers and represent fractions.	MAL3.FR.1a Understand the relationship between different fractions and fractions and decimals. MAL3.FR.1b Interpret a fraction as an answer to a division problem.	
	FR.2		MAL2.FR.2 Order and compare fractions and identify equivalent fractions.	MAL3.FR.2a Build a foundation of addition, subtraction, and multiplication operations with fractions. MAL3.FR.2b Perform operations with	
Algebraic Reasoning (AR)	AR.1	MAL1.AR.1a Solve addition problems with sums between 0 and 20 and subtraction problems using related facts.	MAL2.AR.1a Solve addition problems with sums between 0 and 100 and related subtraction problems.	MAL3.AR.1 Represent and solve problems involving the four operations with whole numbers and fractions.	MAL4.AR.1a Apply previous understanding of arithmetic expressions to algebraic expressions in equivalent forms. MAL4.AR.1b Rewrite algebraic expressions in equivalent forms. MAL4.AR.1c Generate equivalent algebraic expressions.
		MAL1.AR.1b Solve addition problems with sums between 0 and 100 and related subtraction problems.	MAL2.AR.1b Solve multiplication and division problems.		
		MAL1.AR.2a Develop an understanding of the equal sign.	MAL2.AR.2a Demonstrate an understanding of equality and addition and subtraction.	MAL3.AR.2 Demonstrate an understanding of equality, operations with whole numbers, the order of operations and equivalent	MAL4.AR.2a Develop an understanding for solving equations and inequalities. Write and solve one-step equations in one variable.

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ipdae BY EDUCATORS FOR EDUCATORS		Horizontal Progression			
		NRS Level 1	NRS Level 2	NRS Level 3	NRS Level 4
Number Sense and Operations (NSO)	NSO.1	MAL1.NSO.1 Understand the place value of two-digit whole numbers.	MAL2.NSO.1 Understand the place value of four-digit whole numbers.	MAL3.NSO.1a Understand the place value of multi-digit numbers. MAL3.NSO.1b Understand the place value of multi-digit numbers with decimals to the thousandths place.	MAL4.NSO.1a Understand negative numbers and absolute value. MAL4.NSO.1b Rewrite rational numbers in equivalent forms (including fractions, mixed numbers, repeating decimals, and percentages) to solve mathematical and real world problems.
	NSO.2	MAL1.NSO.2 Understand addition and subtraction with one- and two-digit whole numbers.	MAL2.NSO.2 Add and subtract multi-digit whole numbers. Understand multiplication and division operations.	MAL3.NSO.2a Understand operations with multi-digit numbers including decimals. MAL3.NSO.2b Add, subtract, multiply and divide multi-digit numbers.	MAL4.NSO.2c Solve problems involving rational numbers, including numbers in scientific notation, and extend the understanding of rational numbers to irrational numbers. MAL4.NSO.2 Add, subtract, multiply and divide rational numbers.
	NSO.3				MAL4.NSO.3 Apply properties of operations to rewrite numbers in equivalent forms.
Fractions (FR)	FR.1		MAL2.FR.1 Understand fractions as numbers and represent fractions.	MAL3.FR.1a Understand the relationship between different fractions and fractions and decimals. MAL3.FR.1b Interpret a fraction as an answer to a division problem.	
	FR.2		MAL2.FR.2 Order and compare fractions and identify equivalent fractions.	MAL3.FR.2a Build a foundation of addition, subtraction, and multiplication operations with fractions. MAL3.FR.2b Perform operations with	
Algebraic Reasoning (AR)	AR.1	MAL1.AR.1a Solve addition problems with sums between 0 and 20 and subtraction problems using related facts.	MAL2.AR.1a Solve addition problems with sums between 0 and 100 and related subtraction problems.	MAL3.AR.1 Represent and solve problems involving the four operations with whole numbers and fractions.	MAL4.AR.1a Apply previous understanding of arithmetic expressions to algebraic expressions in equivalent forms. MAL4.AR.1b Rewrite algebraic expressions in equivalent forms. MAL4.AR.1c Generate equivalent algebraic expressions.
		MAL1.AR.1b Solve addition problems with sums between 0 and 100 and related subtraction problems.	MAL2.AR.1b Solve multiplication and division problems.		
	MAL1.AR.2a Develop an understanding of the equal sign.	MAL2.AR.2a Demonstrate an understanding of equality and addition and subtraction.	MAL3.AR.2 Demonstrate an understanding of equality, operations with whole numbers, the order of operations and equivalent	MAL4.AR.2a Develop an understanding for solving equations and inequalities. Write and solve one-step equations in one variable.	

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Think-Pair-Share

## How could we use the matrices in our adult education programs?



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Applications

**Instructional Considerations**

- Prior knowledge might students need
- Connections within and across the skills and knowledge within a strand
- Checklist
- Scaffolding
- Chunking
- Differentiating
- Anticipating struggle points
- Closing achievement gaps
- Planning interventions
- Student grouping

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		NRS Level 1	NRS Level 2	NRS Level 3	NRS Level 4
Number Sense and Operations (NSO)	NSO.1	MAL1.NSO.1 Understand the place value of two-digit whole numbers.  <b>WEEK 1</b>	MAL2.NSO.1 Understand the place value of four-digit whole numbers.  <b>WEEK 11</b>	MAL3.NSO.1a Understand the place value of multi-digit numbers. MAL3.NSO.1b Understand the place value of multi-digit numbers with decimals to the thousandths place. MAL3.NSO.1c Rewrite numbers in equivalent forms.	MAL4.NSO.1a Understand negative numbers and absolute value. MAL4.NSO.1b Rewrite rational numbers in equivalent forms (including fractions, mixed numbers, repeating decimals, and percentages) to solve mathematical and real world problems. MAL4.NSO.1c Solve problems involving rational numbers, including numbers in scientific notation, and extend the understanding of rational numbers to irrational numbers.
	NSO.2	MAL1.NSO.2 Understand addition and subtraction with one- and two-digit whole numbers.  <b>WEEK 1</b>	MAL2.NSO.2 Add and subtract multi-digit whole numbers. Understand multiplication and division operations.  <b>WEEK 11</b>	MAL3.NSO.2a Understand operations with multi-digit numbers including decimals. MAL3.NSO.2b Add, subtract, multiply and divide multi-digit numbers.	MAL4.NSO.2 Add, subtract, multiply and divide rational numbers.
	NSO.3				MAL4.NSO.3 Apply properties of operations to rewrite numbers in equivalent forms.
Fractions (FR)	FR.1		MAL2.FR.1 Understand fractions as numbers and represent fractions.  <b>WEEK 12</b>	MAL3.FR.1a Understand the relationship between different fractions and fractions and decimals. MAL3.FR.1b Interpret a fraction as an answer to a division problem.	
	FR.2		MAL2.FR.2 Order and compare fractions and identify equivalent fractions.  <b>WEEK 12</b>	MAL3.FR.2a Build a foundation of addition, subtraction, and multiplication operations with fractions. MAL3.FR.2b Perform operations with	
Algebraic Reasoning (AR)	AR.1	MAL1.AR.1a Solve addition problems with sums between 0 and 20 and subtraction problems using related facts.  <b>WEEK 2</b>	MAL2.AR.1a Solve addition problems with sums between 0 and 100 and related subtraction problems.  <b>WEEK 13</b>	MAL3.AR.1 Represent and solve problems involving the four operations with whole numbers and fractions.	MAL4.AR.1a Apply previous understanding of arithmetic expressions to algebraic expressions in equivalent forms. MAL4.AR.1b Rewrite algebraic expressions in equivalent forms. MAL4.AR.1c Generate equivalent algebraic expressions.
		MAL1.AR.1b Solve addition problems with sums between 0 and 100 and related subtraction problems.  <b>WEEK 2</b>	MAL2.AR.1b Solve multiplication and division problems.  <b>WEEK 13</b>		
		MAL1.AR.2a Develop an understanding of the equal sign.  <b>WEEK 3</b>	MAL2.AR.2a Demonstrate an understanding of equality and addition and subtraction.	MAL3.AR.2 Demonstrate an understanding of equality, operations with whole numbers, the order of operations and equivalent	MAL4.AR.2a Develop an understanding for solving equations and inequalities. Write and solve one-step equations in one variable.

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ipdae BY EDUCATORS FOR EDUCATORS		Scaffolding and Differentiation			
		NRS Level 1	NRS Level 2	NRS Level 3	NRS Level 4
Number Sense and Operations (NSO)	NSO.1	MA.L1.NSO.1 Understand and the place value of two-digit whole numbers.	MA.L2.NSO.1 Understand and the place value of four-digit whole numbers.	MA.L3.NSO.1a Understand and the place value of multi-digit numbers. MA.L3.NSO.1b Understand and the place value of multi-digit numbers with decimals to the thousandth place. MA.L3.NSO.1c Rewrite numbers in equivalent forms.	MA.L4.NSO.1a Understand and negative numbers and absolute value. MA.L4.NSO.1b Rewrite rational numbers in equivalent forms (including fractions, mixed numbers, repeating decimals, and percentages)
	NSO.2	MA.L1.NSO.2 Understand addition and subtraction with one- and two-digit whole numbers.	MA.L2.NSO.2 Add and subtract multi-digit whole numbers. Understand multiplication and division operations.	MA.L3.NSO.2a Understand and operations with multi-digit numbers including decimals. MA.L3.NSO.2b Add, subtract, multiply and divide multi-digit numbers.	MA.L4.NSO.2 Add, subtract, multiply and divide rational numbers.
	NSO.3				MA.L4.NSO.3 Apply properties of operations to rewrite numbers in equivalent forms.
Fractions (FR)	FR.1		MA.L2.FR.1 Understand and fractions as numbers and represent fractions.	MA.L3.FR.1a Understand and the relationship between different fractions and fractions and MA.L3.FR.1b Interpret a fraction as an answer to a division problem.	
	FR.2		MA.L2.FR.2 Order and compare fractions and identify equivalent fractions.	MA.L3.FR.2a Build a foundation of addition, subtraction, and multiplication operations with fractions. MA.L3.FR.2b Perform operations with fractions.	
Algebraic Reasoning (AR)	AR.1	MA.L1.AR.1a Solve addition problems with sums between 0 and 20 and subtraction problems using related facts.	MA.L2.AR.1a Solve addition problems with sums between 0 and 100 and related subtraction problems.	MA.L3.AR.1 Represent and solve problems involving the four operations with whole numbers and fractions.	MA.L4.AR.1a Apply previous understanding of arithmetic expressions to algebraic expressions. MA.L4.AR.1b Rewrite algebraic expressions in equivalent forms. MA.L4.AR.1c Generate equivalent algebraic expressions.
		MA.L1.AR.1b Solve addition problems with sums between 0 and 100 and related subtraction problems.	MA.L2.AR.1b Solve multiplication and division problems.		
	AR.2	MA.L1.AR.2a Develop an understanding of the equal sign.	MA.L2.AR.2a Demonstrate an understanding of equality and addition and subtraction.	MA.L3.AR.2 Demonstrate an understanding of equality, operations with whole numbers, the order of operations and equivalent numerical expressions.	MA.L4.AR.2a Develop an understanding for solving equations and inequalities. Write and solve equations and inequalities in one variable. MA.L4.AR.2b Write and solve equations and inequalities in one variable. MA.L4.AR.2c Solve multi-step one-variable equations and inequalities.
		MA.L1.AR.2b Understand and the relationship between addition and subtraction.	MA.L2.AR.2b Develop an understanding of equality and multiplication and division.		

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ipdae BY EDUCATORS FOR EDUCATORS		Progression			
		NRS Level 1	NRS Level 2	NRS Level 3	NRS Level 4
Number Sense and Operations (NSO)	NSO.1	MA.L1.NSO.1 Understand and the place value of two-digit whole numbers.	MA.L2.NSO.1 Understand and the place value of four-digit whole numbers.	MA.L3.NSO.1a Understand and the place value of multi-digit numbers. MA.L3.NSO.1b Understand and the place value of multi-digit numbers with decimals to the thousandth place. MA.L3.NSO.1c Rewrite numbers in equivalent forms.	MA.L4.NSO.1a Understand and negative numbers and absolute value. MA.L4.NSO.1b Rewrite rational numbers in equivalent forms (including fractions, mixed numbers, repeating decimals, and percentages)
	NSO.2	MA.L1.NSO.2 Understand addition and subtraction with one- and two-digit whole numbers.	MA.L2.NSO.2 Add and subtract multi-digit whole numbers. Understand multiplication and division operations.	MA.L3.NSO.2a Understand and operations with multi-digit numbers including decimals. MA.L3.NSO.2b Add, subtract, multiply and divide multi-digit numbers.	MA.L4.NSO.2 Add, subtract, multiply and divide rational numbers.
	NSO.3				MA.L4.NSO.3 Apply properties of operations to rewrite numbers in equivalent forms.
Fractions (FR)	FR.1		MA.L2.FR.1 Understand and fractions as numbers and represent fractions.	MA.L3.FR.1a Understand and the relationship between different fractions and fractions and MA.L3.FR.1b Interpret a fraction as an answer to a division problem.	
	FR.2		MA.L2.FR.2 Order and compare fractions and identify equivalent fractions.	MA.L3.FR.2a Build a foundation of addition, subtraction, and multiplication operations with fractions. MA.L3.FR.2b Perform operations with fractions.	
Algebraic Reasoning (AR)	AR.1	MA.L1.AR.1a Solve addition problems with sums between 0 and 20 and subtraction problems using related facts.	MA.L2.AR.1a Solve addition problems with sums between 0 and 100 and related subtraction problems.	MA.L3.AR.1 Represent and solve problems involving the four operations with whole numbers and fractions.	MA.L4.AR.1a Apply previous understanding of arithmetic expressions to algebraic expressions. MA.L4.AR.1b Rewrite algebraic expressions in equivalent forms. MA.L4.AR.1c Generate equivalent algebraic expressions.
		MA.L1.AR.1b Solve addition problems with sums between 0 and 100 and related subtraction problems.	MA.L2.AR.1b Solve multiplication and division problems.		
	AR.2	MA.L1.AR.2a Develop an understanding of the equal sign.	MA.L2.AR.2a Demonstrate an understanding of equality and addition and subtraction.	MA.L3.AR.2 Demonstrate an understanding of equality, operations with whole numbers, the order of operations and equivalent numerical expressions.	MA.L4.AR.2a Develop an understanding for solving equations and inequalities. Write and solve equations and inequalities in one variable. MA.L4.AR.2b Write and solve equations and inequalities in one variable. MA.L4.AR.2c Solve multi-step one-variable equations and inequalities.
		MA.L1.AR.2b Understand and the relationship between addition and subtraction.	MA.L2.AR.2b Develop an understanding of equality and multiplication and division.		


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ipdae BY EDUCATORS FOR EDUCATORS		Checklist			
		NRS Level 1	NRS Level 2	NRS Level 3	NRS Level 4
Number Sense and Operations (NSO)	NSO.1	MAL1.NSO.1 Understand the place value of two-digit whole numbers.	MAL2.NSO.1 Understand the place value of four-digit whole numbers.	MAL3.NSO.1a Understand the place value of multi-digit numbers. MAL3.NSO.1b Understand the place value of multi-digit numbers with decimals to the thousandths place.	MAL4.NSO.1a Understand negative numbers and absolute value. MAL4.NSO.1b Rewrite rational numbers in equivalent forms (including fractions, mixed numbers, repeating decimals, and percentages) to solve mathematical and real world problems.
	NSO.2	MAL1.NSO.2 Understand addition and subtraction with one- and two-digit whole numbers.	MAL2.NSO.2 Add and subtract multi-digit whole numbers. Understand multiplication and division operations.	MAL3.NSO.2a Understand operations with multi-digit numbers including decimals. MAL3.NSO.2b Add, subtract, multiply and divide multi-digit numbers.	MAL4.NSO.2c Solve problems involving rational numbers, including numbers in scientific notation, and extend the understanding of rational numbers to irrational numbers. MAL4.NSO.2 Add, subtract, multiply and divide rational numbers.
	NSO.3				MAL4.NSO.3 Apply properties of operations to rewrite numbers in equivalent forms.
Fractions (FR)	FR.1		MAL2.FR.1 Understand fractions as numbers and represent fractions.	MAL3.FR.1a Understand the relationship between different fractions and fractions and decimals. MAL3.FR.1b Interpret a fraction as an answer to a division problem.	
	FR.2		MAL2.FR.2 Order and compare fractions and identify equivalent fractions.	MAL3.FR.2a Build a foundation of addition, subtraction, and multiplication operations with fractions. MAL3.FR.2b Perform operations with	
Algebraic Reasoning (AR)	AR.1	MAL1.AR.1a Solve addition problems with sums between 0 and 20 and subtraction problems using related facts.	MAL2.AR.1a Solve addition problems with sums between 0 and 100 and related subtraction problems.	MAL3.AR.1 Represent and solve problems involving the four operations with whole numbers and fractions.	MAL4.AR.1a Apply previous understanding of arithmetic expressions to algebraic expressions.
		MAL1.AR.1b Solve addition problems with sums between 0 and 100 and related subtraction problems.	MAL2.AR.1b Solve multiplication and division problems.		MAL4.AR.1b Rewrite algebraic expressions in equivalent forms.
	MAL1.AR.2a Develop an understanding of the equal sign.	MAL2.AR.2a Demonstrate an understanding of equality and addition and subtraction.	MAL3.AR.2 Demonstrate an understanding of equality, operations with whole numbers, the order of operations and equivalent	MAL4.AR.2a Develop an understanding for solving equations and inequalities. Write and solve one-step equations in one variable.	

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ipdae BY EDUCATORS FOR EDUCATORS		Benefits to Teachers
		<ul style="list-style-type: none"> <li>• Summarizes the ABE math standards in a more visual representation</li> <li>• Shows an overall picture of the ABE math standards</li> <li>• Shows the logical grouping and possible sequencing of the standards</li> <li>• Emphasizes out how each standards relate to one another</li> <li>• Organizes the standards in ABE levels across conceptual categories/strands</li> <li>• Shows how much content/objectives are covered at each ABE level or strand</li> </ul>

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Benefits to Students

- Serves as a quick guide for teachers so that they are able to prioritize and differentiate teaching to the most important skills to adult students based on the student's ability, curriculum and standardized assessment.
- Enumerates every skill/concept/topic that has to be covered in the ABE Math Classroom.
- Highlights every standard that is tested in standardized assessments, which ones have been mastered versus the ones that are deficient.

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Mathematics Activity Resources

### Mathematics Activity Resource

#### Mathematics Matrix

		NRB Level 1	NRB Level 2
Number Sense and Operations (NSO)	NSO.1	MAL1.NSO.1 Understand the place value of two-digit whole numbers.	MAL2.NSO.1 Understand the place of four-digit whole numbers.
	NSO.2	MAL1.NSO.2 Understand addition and subtraction with one- and two-digit whole numbers.	MAL2.NSO.2 Add and subtract multi-digit whole numbers. Understand multiplication and division operations.
	NSO.3		
Fractions (FR)	FR.1		MAL2.FR.1 Understand fractions as numbers and represent fractions.
	FR.2		MAL2.FR.2 Order and compare fractions and identify equivalent fractions.
Algebraic Reasoning (AR)	AR.1	MAL1.AR.1 Solve addition problems with sums between 0 and 20 and subtraction problems with related facts.	MAL2.AR.1 Solve addition problems with sums between 0 and 100 and related subtraction problems.
	AR.2	MAL1.AR.2a Develop an understanding of the equal sign.	MAL2.AR.2a Demonstrate an understanding of equality and addition subtraction.



Math Resource Order and Compare Fractions MA.L2.FR.2

Misconceptions and Ideas for Understanding Concepts

Students may assume fractions with smaller denominators are smaller than fractions with larger denominators when placing them on a number line.

or not equivalent when referring to the same size whole. Instruction includes partitioning shapes into halves, thirds, and fourths and then comparing the resulting pieces.

For example, students partition a shape into halves.



Conversation includes sharing observations about the shape partitioned into two equal pieces. The teacher models writing the fractional parts of  $\frac{1}{2}$  so that students can connect the number of pieces to the denominator. Students then practice partitioning shapes into thirds and fourths to reinforce the concept.

Explicitly address confusing examples where students may believe that that larger denominator indicates a larger amount. For example:

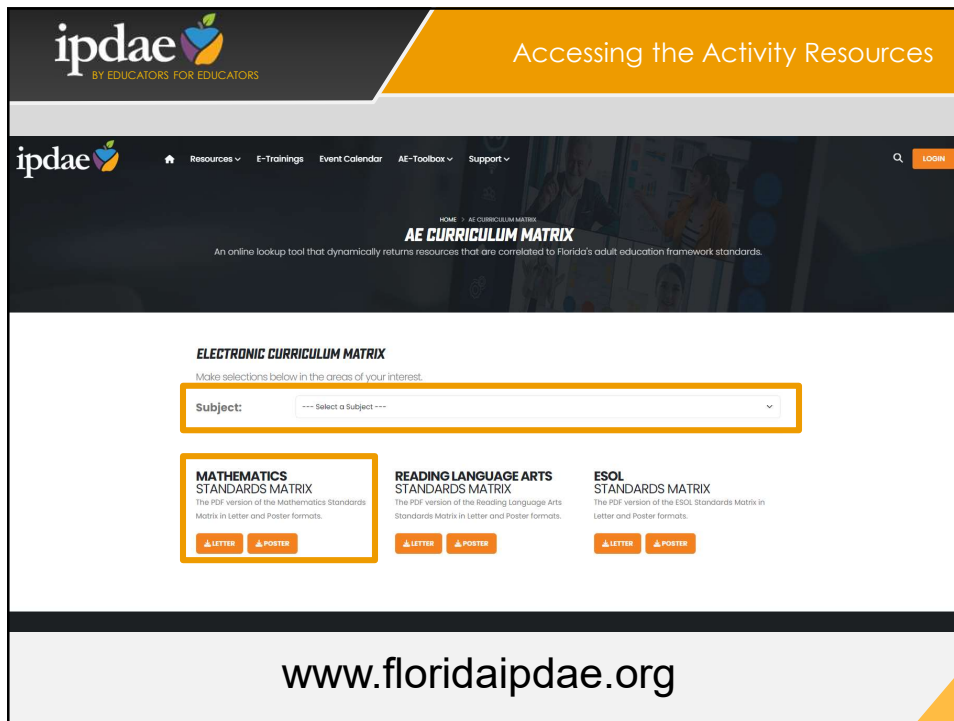
- The corner store sells candy bars that are exactly the same size. Kaitlyn ate  $\frac{1}{4}$  of a candy bar and Jake ate  $\frac{1}{6}$  of a candy bar. Who ate a larger piece?

Emphasize that fractions represent a specific amount that must be determined by comparing the numerator to the denominator. Students need practice experiencing fractions that have larger denominators but that still represent smaller amounts.

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The Amazing Race

**Challenge 1:** Will test your groups ability to recall information

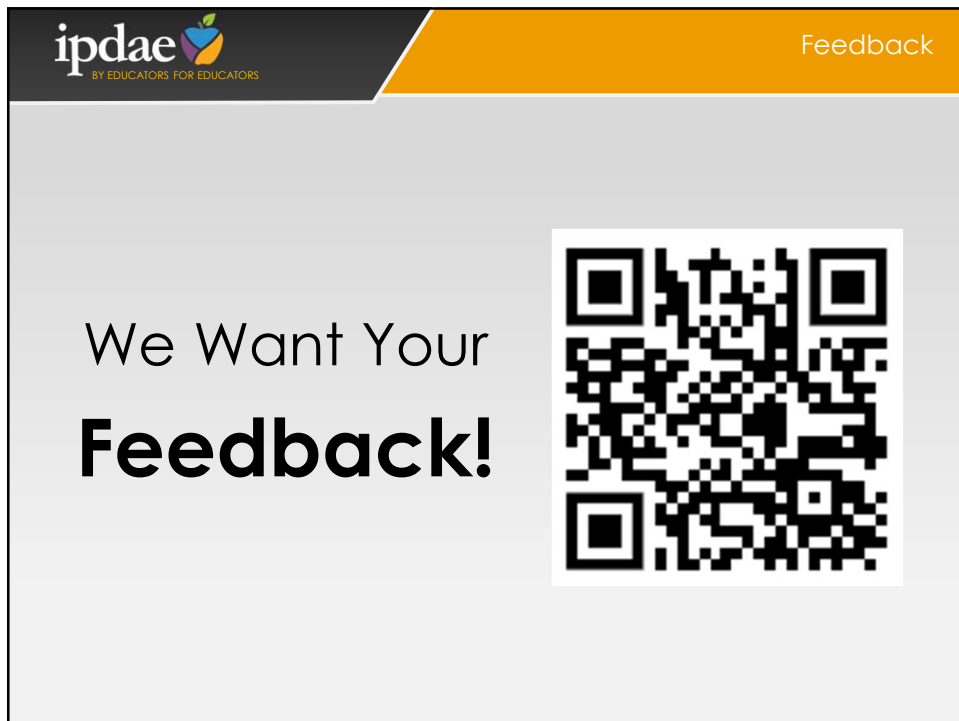
**Challenge 2:** Will test your groups leveling ability

**Challenge 3:** Will test your groups cognitive and fine motor skills

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